

# DILEPTON PRODUCTION IN TRANSPORT MODELS

Janus Weil

Frankfurt Institute for Advanced Studies

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**FIAS** Frankfurt Institute  
for Advanced Studies



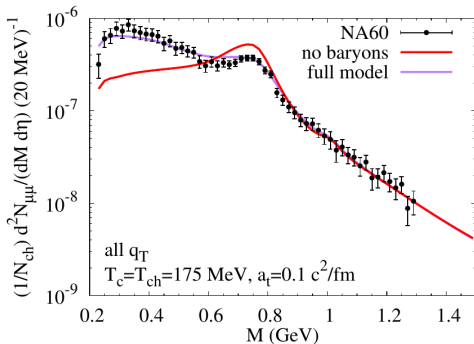
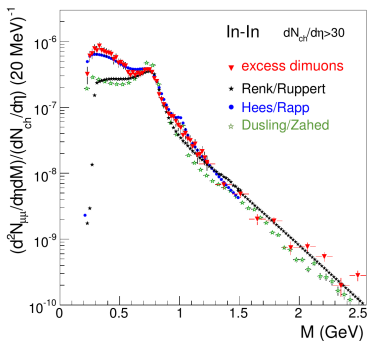
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**HIC** | **FAIR**  
for  
Helmholtz International Center

- general intro
  - what's so interesting about dileptons?
  - vector mesons in medium
- the current state of things
  - what has been done in general
  - some important results
- what we can (and have to) do in a transport approach
- electromagnetic  $\Delta$  transition form factor
  - 2-component model (Ramalho et al)
  - transport treatment: "2-step VMD"
- dileptons with Smash
  - treatment of resonances
  - what it means for dileptons
  - in particular: focus on  $\omega$  meson

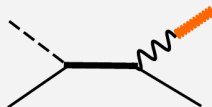
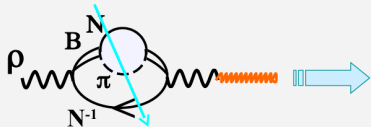
- dileptons ( $e^+e^-$ ,  $\mu^+\mu^-$ ) are an important probe of physics at high densities and temperatures
- only em. interaction, traverse hadronic medium
- “electromagnetic probe for studying QCD physics”
  
- vector mesons carry quantum numbers of a ‘heavy photon’, can directly convert into a lepton pair
- important application of dileptons: observe in-medium spectral function of vector mesons
- naive expectations: broadening or shift of spectral functions at finite density/temperature

- important dimuon experiment at CERN-SPS,  $\sqrt{s} \approx 17$  GeV
- NA60 data showed:  $\rho^0$  spectral function substantially broadened in medium (but essentially no mass shift)
- shown by Rapp/Hees: mainly driven by baryonic effects (coupling to  $N^*$  resonances)

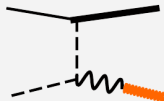
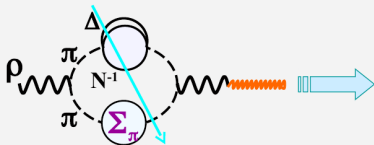


## Production Processes from $\rho$ Spectral Function

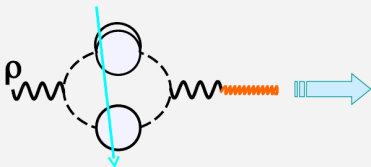
↔ Cuts (imag. parts) of Selfenergy Diagrams:



resonance  
Dalitz decays  
 $\pi N \rightarrow \Delta \rightarrow \gamma N$   
 $\pi \rho \rightarrow a_1 \rightarrow \gamma \pi$



meson-exchange  
scattering  
 $\pi N \rightarrow \gamma N, \gamma \Delta$

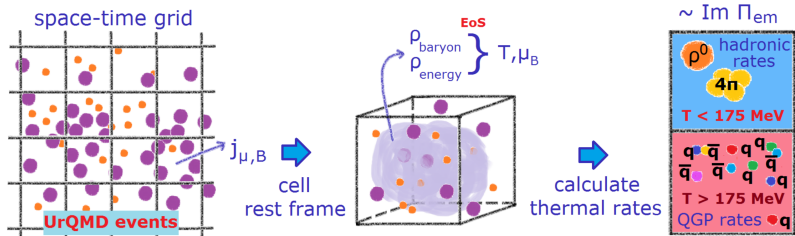


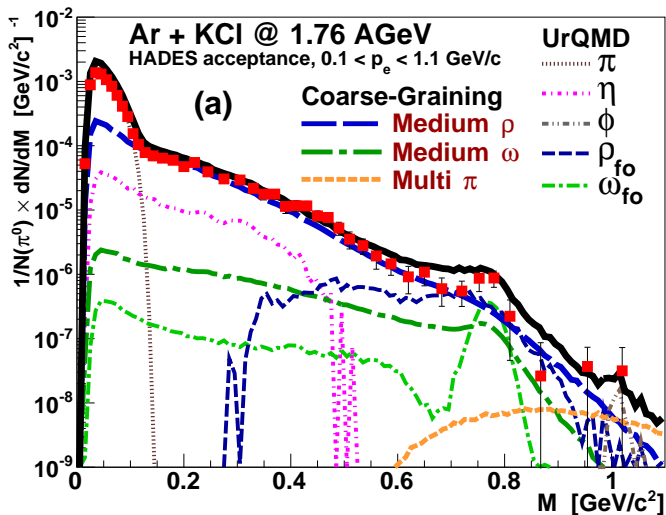
Bremsstrahlung  
 $NN \rightarrow \gamma NN, \gamma N\Delta,$

by Ralf Rapp

# “COARSE GRAINING”

- PhD project of Stephan Endres
- put UrQMD simulation onto space-time grid
- for each cell, determine baryon and energy density
- use equation of state to calculate local temperature and baryo-chemical potential
- calculate thermal dilepton rates using Rapp-Wambach spectral function (Rapp 1997, NPA 617)





S. Endres et al., Phys. Rev. C 92, 014911 (2015)

- a “standard model” for dilepton production has emerged ...
- Rapp/Wambach spectral function can explain dilepton data over a large range of energies (HADES, NA60, STAR, ...)
- most important ingredients: couplings of  $\rho$  meson to baryonic resonances ( $N^*$ ,  $\Delta^*$ )
- many transport models also contain these ingredients (e.g. UrQMD, GiBUU, ..)
- **question:** how far can we get with a transport\* description of dilepton production? (\* microscopical, off-equilibrium)



- basic problem: how to deal with dynamic (i.e. density-dependent) spectral functions
- 'traditional' ansatz: use some externally-provided spectral function (pick your favorite model)
- plug it into the transport model via 'off-shell transport'
- $\Rightarrow$  test-particle masses (representing spectral function) change dynamically with density (even without collisions)

off-shell EOM for test particles:

[Cassing/Juchem (NPA 665, 2000), Leupold (NPA 672, 2000)]:

$$\begin{aligned}\dot{\vec{r}}_i &= \frac{1}{1 - C_i} \frac{1}{2E_i} \left[ 2\vec{p}_i + \frac{\partial}{\partial \vec{p}_i} \text{Re}(\Sigma_i) + \chi_i \frac{\partial \Gamma_i}{\partial \vec{p}_i} \right], \\ \dot{\vec{p}}_i &= -\frac{1}{1 - C_i} \frac{1}{2E_i} \left[ \frac{\partial}{\partial \vec{r}_i} \text{Re}(\Sigma_i) + \chi_i \frac{\partial \Gamma_i}{\partial \vec{r}_i} \right], \\ C_i &= \frac{1}{2E_i} \left[ \frac{\partial}{\partial E_i} \text{Re}(\Sigma_i) + \chi_i \frac{\partial \Gamma_i}{\partial E_i} \right], \\ \chi_i &= \frac{m_i^2 - M^2}{\Gamma_i}, \quad \frac{d\chi_i}{dt} = 0\end{aligned}$$

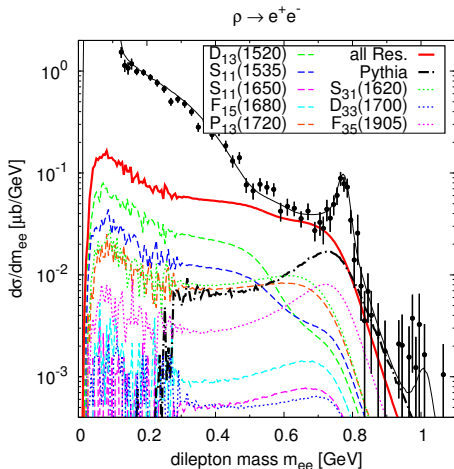
- needed to incorporate density-dependent spectral functions (self energy  $\Sigma_i$ , width  $\Gamma_i \sim \text{Im}(\Sigma_i)$ )
- test particles dynamically change their masses
- but: some approximations required
  - neglecting momentum dependence
  - only works 'close to mass shell'

# SHIFTING THE PARADIGM

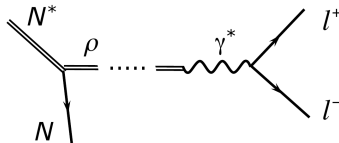
- problem: off-shell transport can only handle 'simple' spectral modifications
- was tried by different people (with different codes):  
M. Effenberger, E. Bratkovskaya, G. Wolf, J.W., ...
- to my knowledge, this approach never actually produced any convincing results
  
- the alternative: focus more on things that can be intrinsically provided by transport, instead of putting in things from the outside
- transport itself can generate many of the relevant effects
- “collisional broadening” via explicit collisions
- 'off-shell transport' may not even be required:  
with sufficient amount of collisions, SF changes dynamically anyway

# RESONANCE EFFECTS

- Dalitz decays of baryonic resonances ( $N^*$ ,  $\Delta^*$ ) give important contributions to dil. spectrum



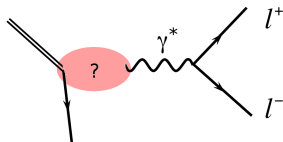
GiBUU simulation of  
pp@3.5GeV, compared to  
HADES data



Weil, Hees, Mosel,  
EPJA 48 (2012) 111

# ELECTROMAGNETIC FORM FACTORS

- in general any em. Dalitz decay includes a transition FF



- FF of most mesonic Dalitz decays fixed by data (NA60)
- $\pi^0, \eta \rightarrow e^+ e^- \gamma$  (Landsberg):

$$F(m) = \left(1 - \frac{m^2}{\Lambda^2}\right)^{-1}$$

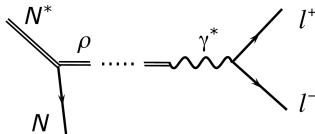
- $\omega \rightarrow e^+ e^- \pi^0$  (Bratkovskaya):

$$F(m) = \frac{\Lambda^4}{(\Lambda^2 - m^2)^2 + \Lambda^2 \Gamma^2}$$

- parameters  $\Lambda, \Gamma$  are fitted to data

# BARYONIC FORM FACTORS & VMD

- em. FFs of the baryons are harder to grasp experimentally
- there are many  $N^*$  and  $\Delta^*$  states, their contributions are hard to disentangle
- it is almost impossible to separate them out of a given data sample
- our ansatz of using  $N^* \rightarrow \rho N \rightarrow e^+ e^- N$  practically corresponds to a vector-meson dominance (VMD) hypothesis
- VMD: “all hadrons couple to the em. sector primarily via vector mesons”
- the two-step procedure does not only provide a mass-dependence, but a full kinematic model of this coupling



# $\Delta$ EM. TRANSITION FF

- what about the  $\Delta(1232)$ ?
- $\Delta$  em. transition FF measured in spacelike region (electron scattering) and at the real-photon point
- we need a model to extend the FF into the time-like region
- $\Delta$  Dalitz decay width (Krivoruchenko et al.):

$$\frac{d\Gamma}{dq} = \frac{2\alpha}{3\pi q} \frac{\alpha}{16} \frac{(W + m_N)^2}{W^3 m_N^2} \sqrt{(W + m_N)^2 - q^2} [(W - m_N)^2 - q^2]^{3/2} |F(q^2, W)|^2$$

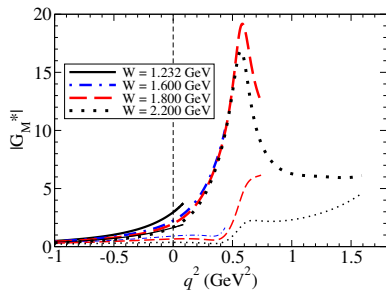
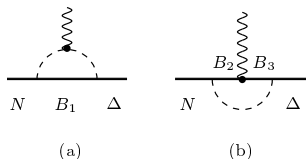
- $q$  = dilepton mass,  $W$  =  $\Delta$  mass
- in principle there are three FFs ( $G_E$ ,  $G_M$ ,  $G_C$ ), but  $G_M$  dominates strongly for the  $\Delta$
- we will try different approaches for the form factor:
  - 'QED' (constant FF, fixed at photon point)
  - two-component model (Ramalho et al)
  - "2-step VMD" (as for  $N^*$ )

# RAMALHO/PEÑA MODEL

- "covariant spectator quark model"
- phenomenological model:  
bare quark core + meson cloud

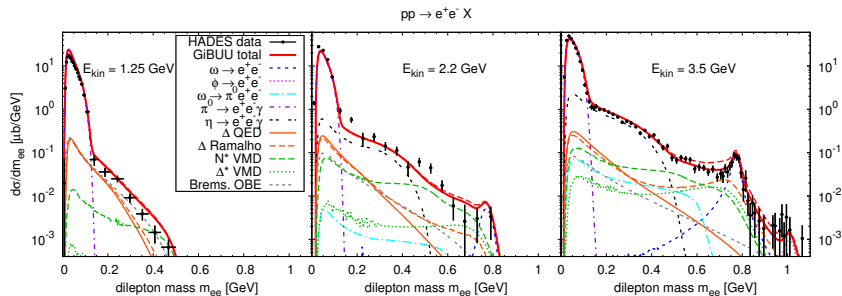
$$G(q^2, W) = G^b(q^2, W) + G^\pi(q^2)$$

- bare quark contribution calibrated with lattice QCD data
- pion-cloud contribution relies on measured pion form factor
- $W$  dependence in pion cloud neglected
- Ramalho et al., arXiv:1512.03764 (accepted for Phys. Rev. D)





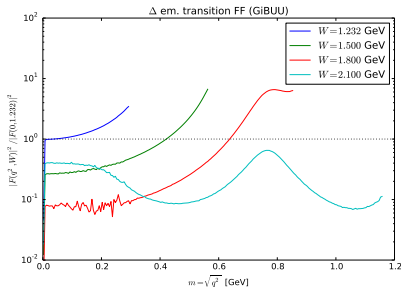
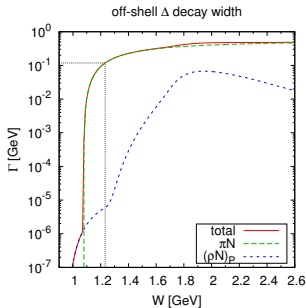
# RESULTS WITH RAMALHO FF



- at low energies FF has only minor influence
- at higher energies it enhances the yield by more than an order of magnitude
- slightly conflicting with HADES data when added to other channels ( $N^*$ ,  $\Delta^*$ )

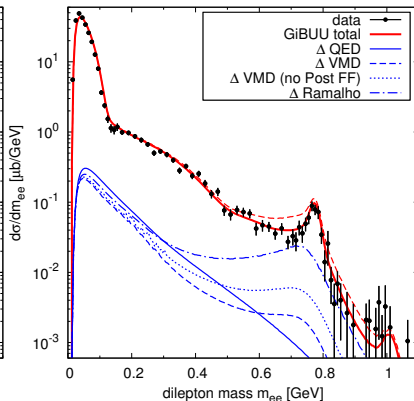
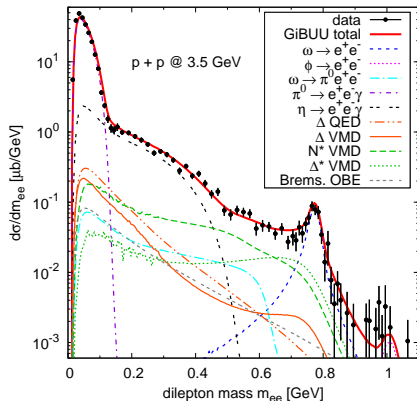
# 2-STEP VMD: $\rho$ - $\Delta$ COUPLING

- $\Delta \rightarrow \rho N$  coupling can not be directly inferred from PWA of  $\pi N \rightarrow 2\pi N$  data
- $\Delta$  is too light to decay into  $\rho N$  (on the mass shell)
- but: off-shell  $\Delta$  can decay into off-shell  $\rho$
- this coupling can be important for dilepton spectra
- we introduce a p-wave decay with an (on-shell) BR of  $5 \cdot 10^{-5}$
- $\rightarrow$  consistent 2-step VMD approach for all baryons

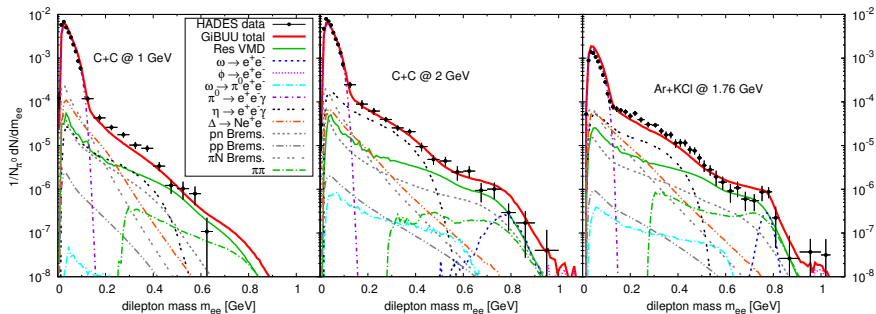


# RESULTS WITH 2-STEP VMD APPROACH

- VMD vs Ramalho model
- result: very similar dependence on  $q^2$  (i.e. dilepton mass)
- but: different  $W$  dependence (apparently important!)



# HEAVY IONS WITH GiBUU



- once the elementary p+p collisions are all properly described, also A+A comes out rather well (but not perfect)
- not much room for additional modifications left (a la off-shell transport), but maybe a bit

- 2-step VMD treatment is a reasonable ansatz for baryons
- probably the best we can do in a transport approach for now
- seems compatible with basically all the dilepton data measured by HADES
- some details yet to be clarified (coupling constants for particular resonances, etc)

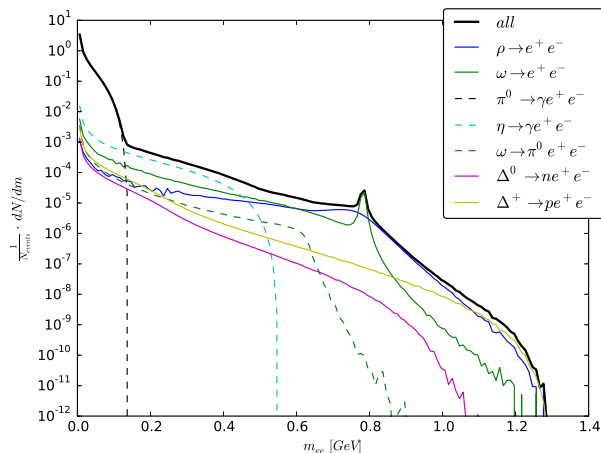
- SMASH: new hadronic transport model developed in group of Hannah Petersen
- still "in the making" (currently v0.9), but already yields some interesting results
- results shown here: so far only qualitative, need to be worked out further (no detector acceptance yet, etc)
- dilepton implementation started by Jan Staudenmaier (as BSc project)



# SMASH: RESONANCE IMPLEMENTATION

- primary particle production mechanisms in few-GeV regime:
  - $NN \rightarrow B_1 B_2$
  - $\pi N \rightarrow B$
- with baryons  $B = N, N^*, \Delta, \Delta^*$
- essentially all mesons ( $m = \pi, \eta, \rho, \omega, \dots$ ) produced via  $B^*$  decays,  $B^* \rightarrow mN$  etc
- model currently only contains  $1 \leftrightarrow 2$  and  $2 \leftrightarrow 2$  processes (in order to strictly fulfill detailed balance)
- no string fragmentation yet
- $\omega$  meson:
  - dominantly decays into  $3\pi$  ( $\sim 90\%$ )
  - $\omega \rightarrow 3\pi$  emulated by decay chain  $\omega \rightarrow \rho\pi \rightarrow 3\pi$  in Smash

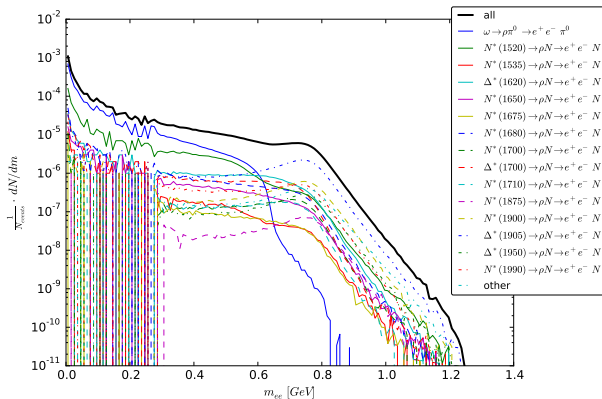
# EXAMPLE SPECTRUM: P+P @ 3.5 GeV



- most channels as expected (std Dalitz decays etc)
- $\rho$  includes Dalitz-like contributions from  $N^*$  decays
- most surprising:  $\omega$

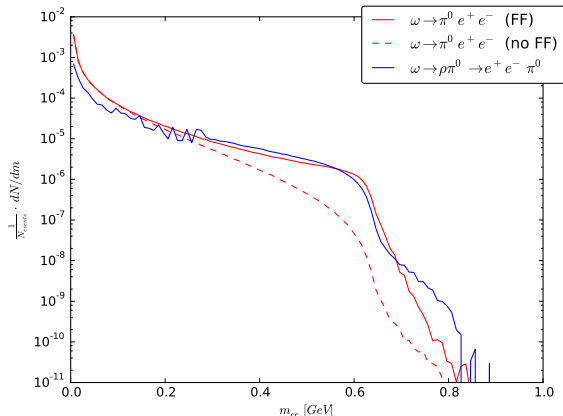


# $\rho$ -LIKE CONTRIBUTIONS ( $B^*$ DALITZ DECAYS)



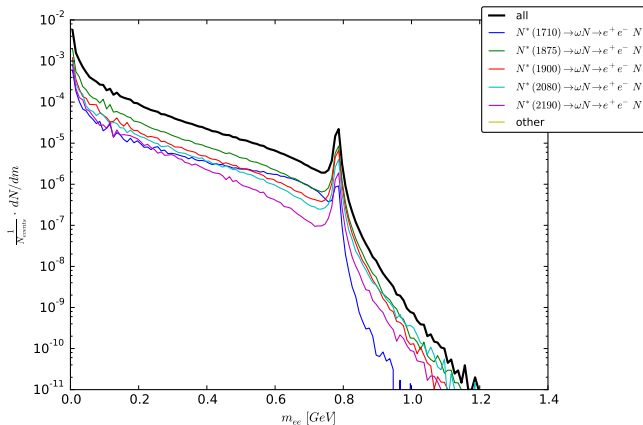
- whole cocktail of  $N^*$  and  $\Delta^*$  decays
- different shapes (mostly determined by res. mass)
- plus: "feed-down" from  $\omega$  (aka  $\omega$  Dalitz decay)

# $\omega$ DALITZ DECAY



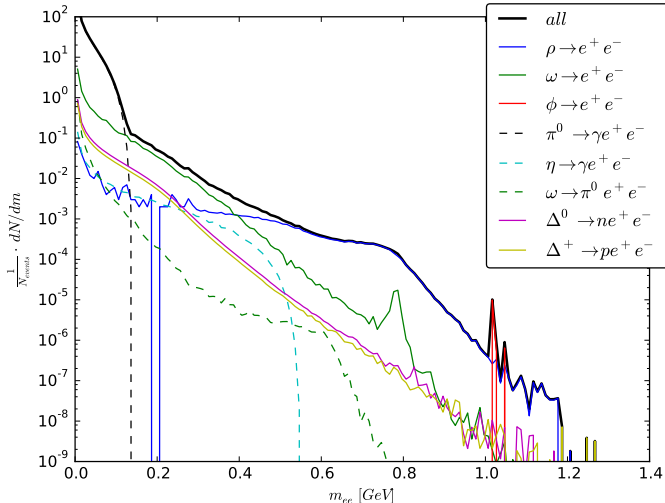
- red: Dalitz decay with FF (FF: fit to data by E. Bratkovskaya)
- blue: 2-step decay via  $\rho$
- both are reasonably similar, but do not agree fully
- to do: compare to NA60 data for  $\omega$  FF

# $\omega$ -LIKE CONTRIBUTIONS ( $N^*$ DALITZ DECAYS)



- again: contributions from several  $N^*$  resonances
- structure: peak at  $\omega$  pole mass, plus Dalitz-like tail

# OUTLOOK: AU+AU @ 1.25 GeV



- fully dominated by baryonic Dalitz decays via  $\rho$  and  $\omega$
- preliminary! further checks required ...

- 2-step VMD approach shows good results for  $\omega$  Dalitz FF
- also seems like a reasonable ansatz for the  $\Delta$  (as well as  $N^*$ ,  $\Delta^*$ )
- em. Dalitz decays of  $N^*$  resonances not only through  $\rho$ , but also through  $\omega$  meson
  
- to do for Smash:
  - apply detector acceptance
  - compare to pp data
  - possibly adjust some res. properties (branching ratios etc)
  - look at heavy-ion data
  - cross-check with pion beam