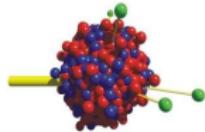


One-pion production
in electron and neutrino scattering on nuclei

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Justus-Liebig University Giessen, Germany



GiBUU

The Giessen Boltzmann-Uehling-Uhlenbeck Project

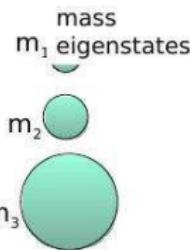
Institut für Theoretische Physik, JLU Giessen

Why to study neutrino-nucleus interactions

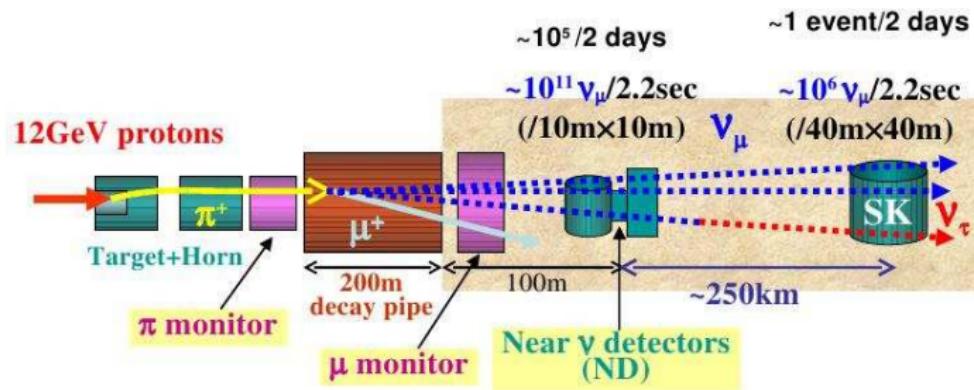
Weak eigenstates



$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U_{\text{MNS}} V_M^{\text{CP}} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$



Long baseline experiments: (K2K — KEK to Kamiokande)

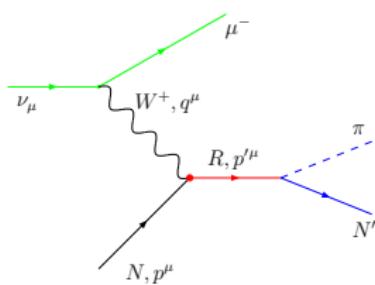


Nearby and faraway detectors: different nuclei as targets, the x-sec did not cancel
background processes are different

One pion production as resonances + background

Neutrino energies > 0.5 GeV
typical xsec $\sim \text{few} \cdot 10^{-38} \text{ cm}^2$

$\nu p \rightarrow \mu^- p \pi^+$ can be described by isobar diagram
as production of $\Delta = P_{33}(1232)$ baryon resonance



Two other channels $\nu n \rightarrow \mu^- p \pi^0$,
 $\nu n \rightarrow \mu^- n \pi^+$

Isospin=1/2 resonances also contribute:
 $P_{11}(1440)$, $D_{13}(1520)$, $S_{11}(1535)$

Theoretical curves are still < the experimental data
→ background is needed

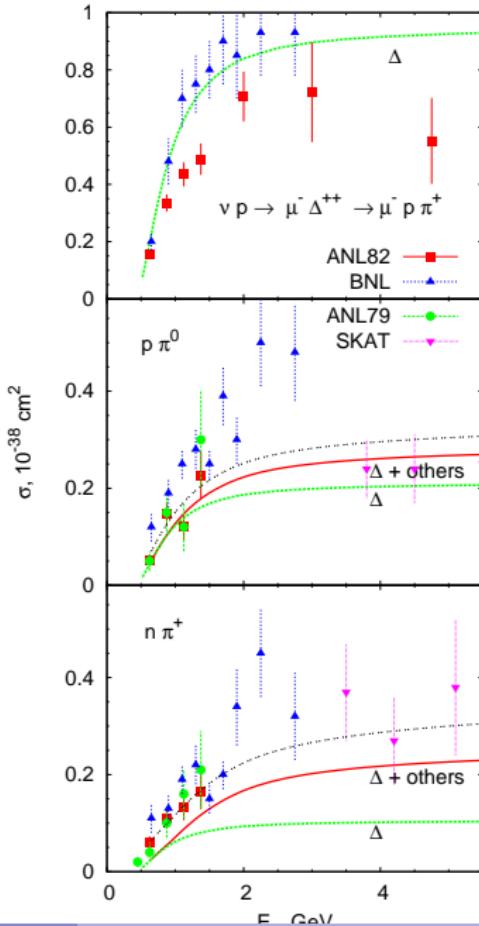
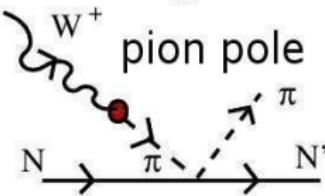
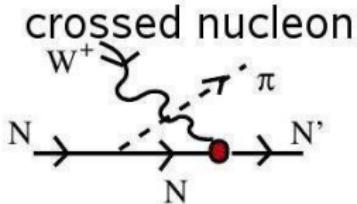
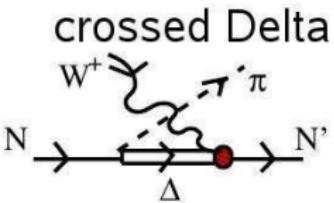
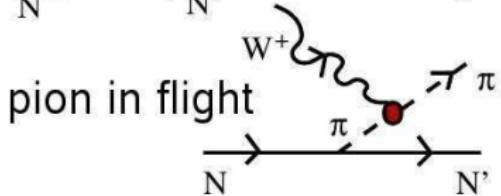
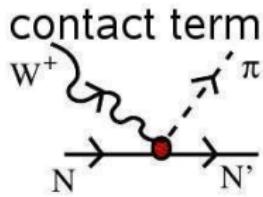
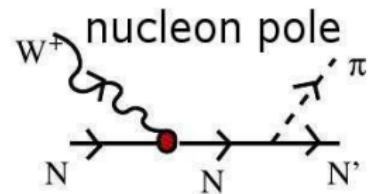
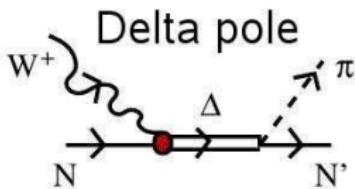


Diagram approach to the 1-pion production

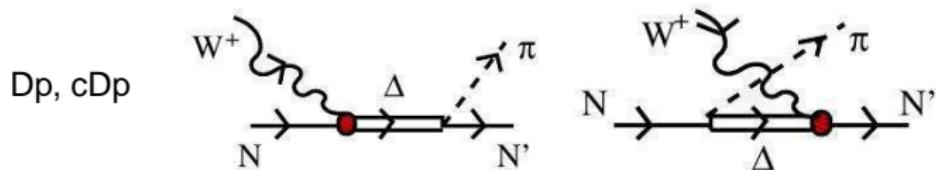


Earlier: only
Delta pole (Dp)
diagram

“Background” as
exper data — Dp

Vertices from $SU(2)$ non-linear sigma-model

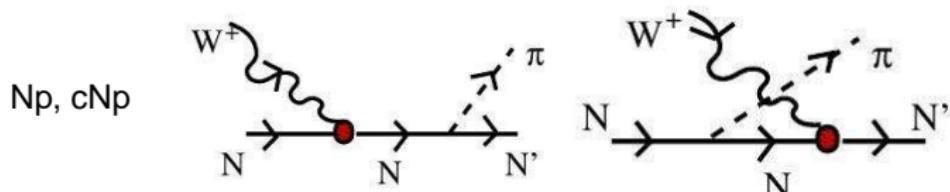
phenomenologically extended by introducing form factors, but **NO** new adjustable parameters



$WN\Delta$: standard parameterization with the form factors

$\Delta N\pi$: standard parameterization

with the coupling constant determined from the Γ_{tot}



$WN'N'$: point-like vertex extended with the nucleon form factors

$$\mathcal{L} = W_\mu^\alpha \bar{N} \gamma^\mu (1 + g_A \gamma_5) \frac{\tau_a}{2} N \otimes \text{nucleon form factors}$$

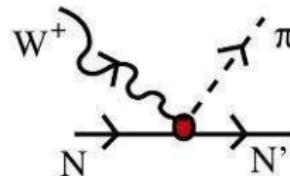
$$\mathcal{L} = \frac{g_A}{2f_\pi} \bar{N} \gamma^\mu \gamma^5 \tau_a \partial_\mu \pi_a N$$

from $SU(2)$ non-linear σ -model

Vertices from non-linear sigma-model

Constants $g_A = 1.23$, $f_\pi = 0.097 \text{ GeV}$, form factors $F_\rho = 1/(1 + Q^2/m_\rho^2)$,
from vector current conservation $F_{CT} = F_{pF}$ coincide with nucleon FF F_1^ν .

CT (contact term)

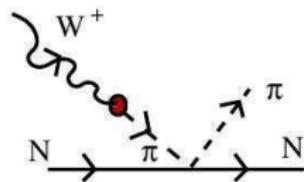


including ρ -dominance

$WNN'\pi$:

$$\mathcal{L} = \frac{1}{2f_\pi} \bar{N} \gamma^\mu W_\mu^a \varepsilon_{abc} \pi_b \tau_c N \cdot \mathbf{F}_\rho - \frac{g_A}{2f_\pi} \bar{N} \gamma^\mu \gamma^5 W_\mu^a \varepsilon_{abc} \pi_b \tau_c N \cdot \mathbf{F}_{CT}$$

pp (pion pole)



including ρ -dominance

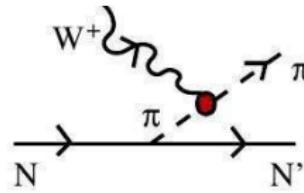
$WNN'\pi$:

$$\mathcal{L} = -W_a^\mu f_\pi \partial_\mu \pi^a$$

$NN'\pi\pi'$:

$$\mathcal{L} = -\frac{1}{4f_\pi^2} \bar{N} \gamma^\mu \varepsilon_{abc} \tau_a \pi_b \partial_\mu \pi_c N \cdot \mathbf{F}_\rho$$

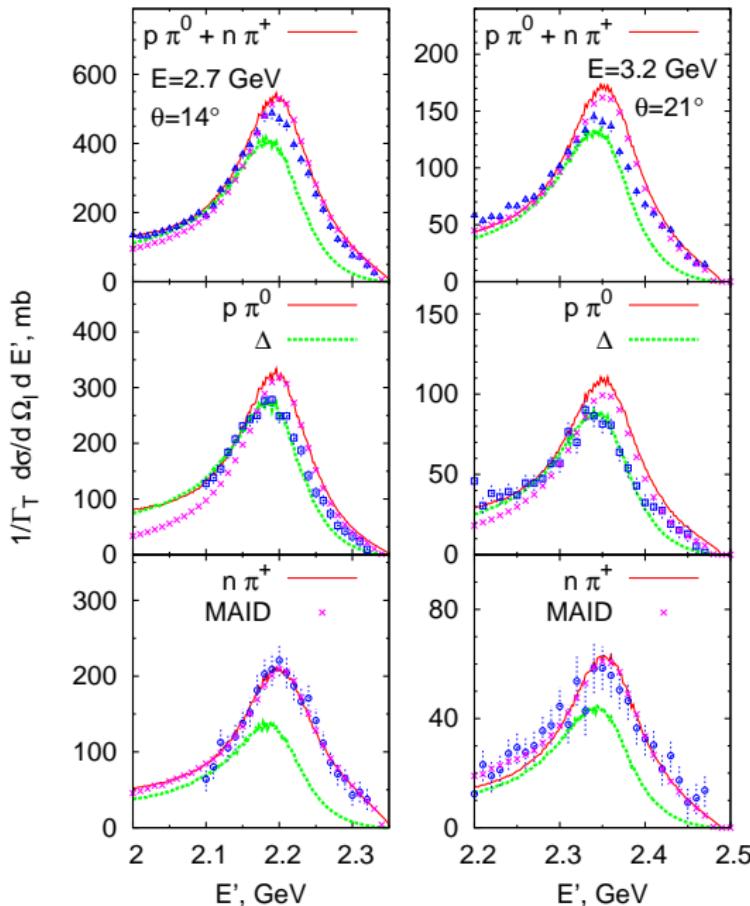
pF (pion in Flight)



$W\pi\pi'$:

$$\mathcal{L} = W_a^\mu \varepsilon_{abc} \pi_b \partial_\mu \pi_c \cdot \mathbf{F}_{pF}$$

Electroproduction as benchmark for neutrino production



The same theoretical input
but axial part = 0

$$ep \rightarrow e \ p\pi^0 \\ n\pi^+$$

Electroproduction data Galster,
1973

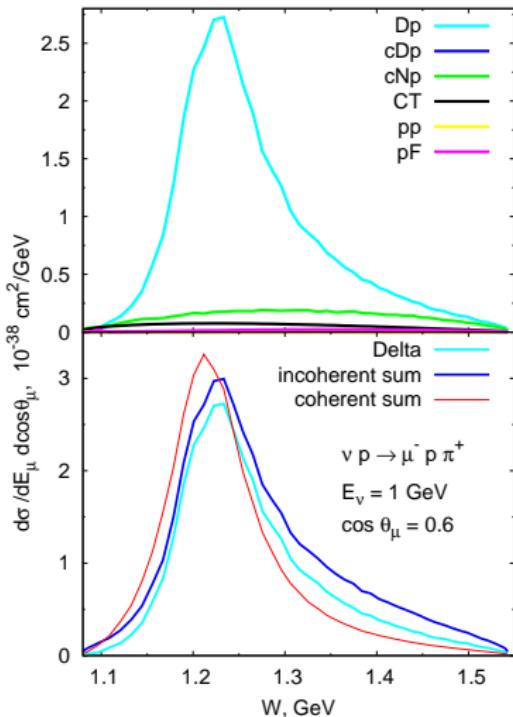
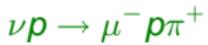
$$\frac{1}{\Gamma_T} \frac{d\sigma}{d\Omega_I dE'} = \sigma_T + \varepsilon \sigma_L$$

are described at the same level
of accuracy as MAID

(a Unitary Isobar Model for Pion
Photo- and Electroproduction on
the Nucleon)

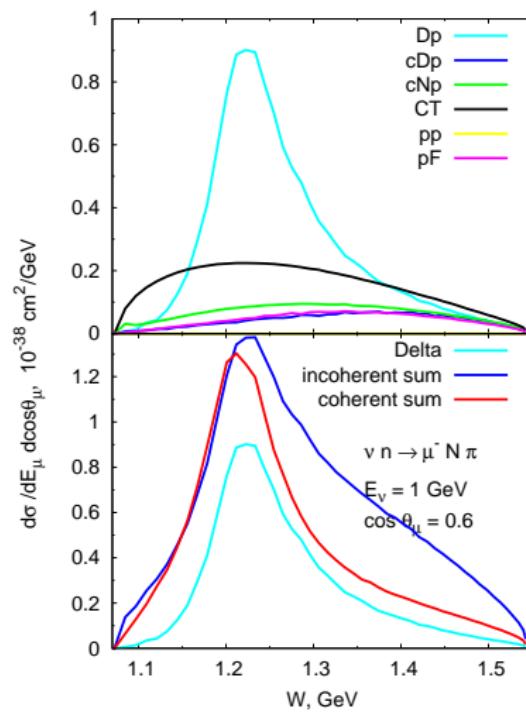
Drechsel et al (Mainz group)
2007

Neutrino–proton



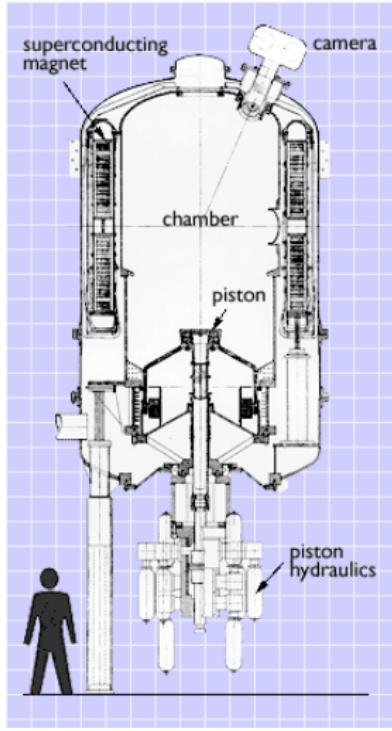
consistent with negligible background

Neutrino-neutron



consistent with earlier expectations

Wide-band-beam neutrino experiments on hydrogen and deuterium



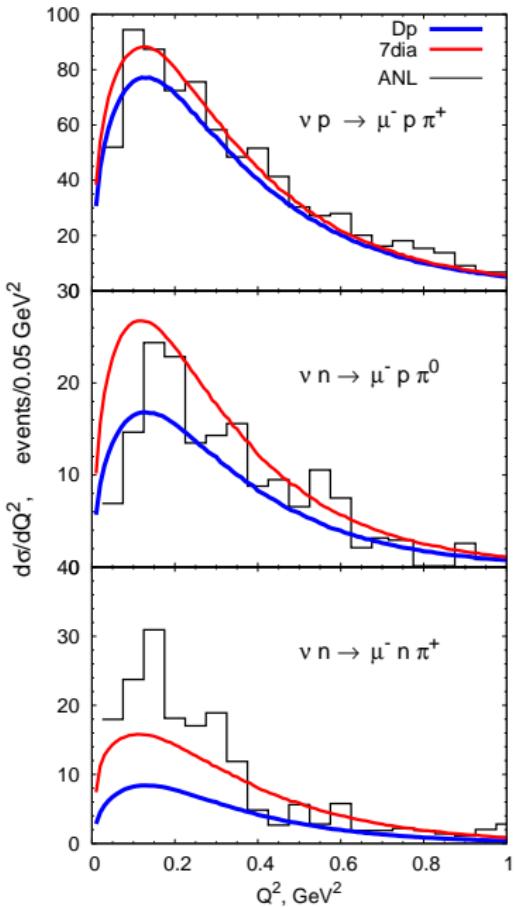
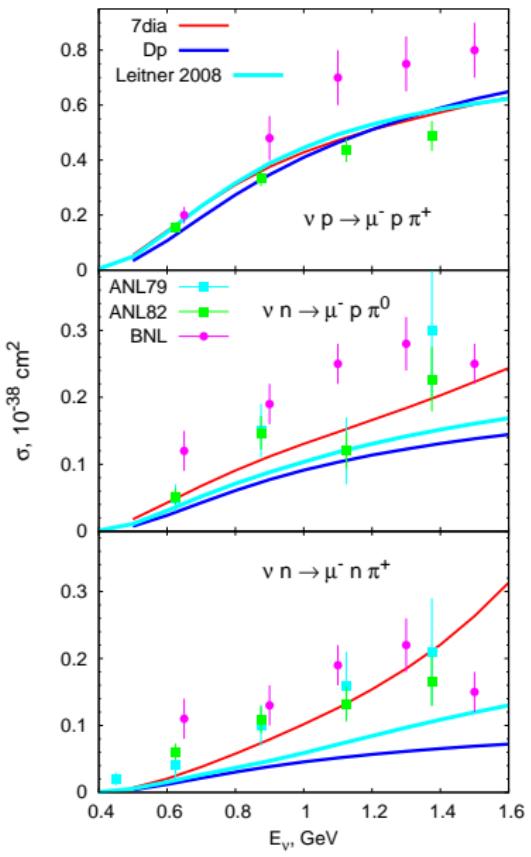
NO modern experiments on protons (hydrogen target) and neutrons (deuterium target)

Old experiments

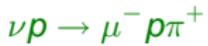
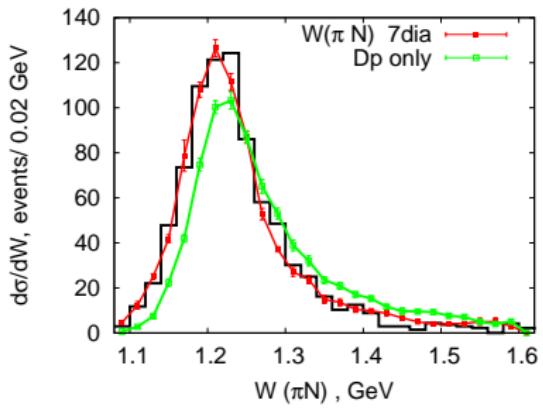
ANL : Argonne National Laboratory 12-ft bubble chamber, 1970 – 80s experiments with hydrogen and deuterium, $\langle E_\nu \rangle \sim 0.9$ GeV

BNL : Brookhaven National Laboratory 7-ft bubble chamber, 1974– 90s experiments with deuterium, $\langle E_\nu \rangle \sim 1.6$ GeV

Neutrino–nucleon interactions

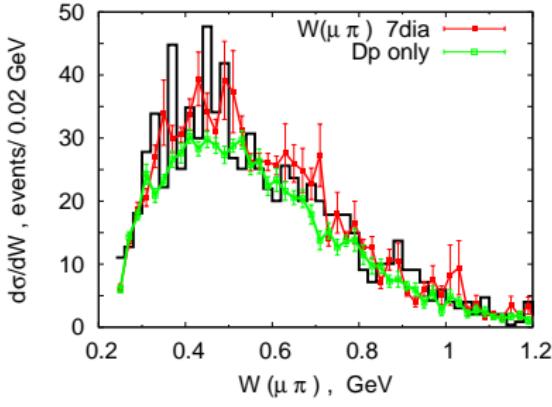
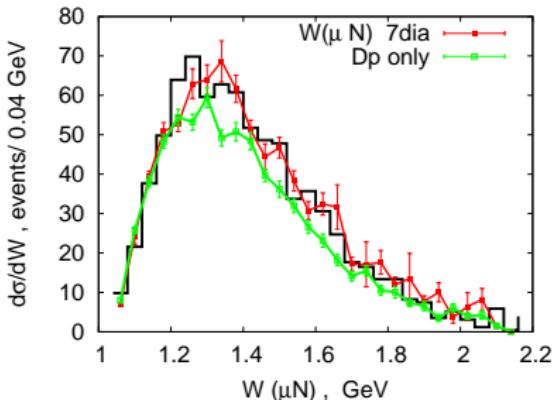


Various invariant mass distributions



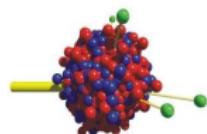
$W(\mu N)$ and $W(\mu \pi)$ distributions calculated theoretically for the first time

experimental data — ANL



Neutrino–nucleus interactions

The nuclear effects (**initial** and **final** state interactions) are described within



GiBUU

The Giessen Boltzmann-Uehling-Uhlenbeck Project

Institut für Theoretische Physik, JLU Giessen

GiBUU — the semiclassical transport model in coupled channels — simulates the transport of hadrons through nuclear matter in space and time

GiBUU describes several reactions both in resonance and high energy regions:

- heavy ion collisions AA
- pion–induced reactions πA
- photon–induced reactions γA
- electron–induced reactions $e^- A$
- neutrino–induced reactions νA
 - ▶ pole mechanism for resonances (13 resonances) + MAID–based phenomenological model for noninterfering background
 - ▶ Hernandez–Nieves–Valverde model of **Delta + background** through several diagrams, including interference effects

Open source code: <http://gibuu.physik.uni-giessen.de/GiBUU/>

Conclusion and Outlook

- Accurate knowledge of neutrino–nucleus interactions is prerequisite for modern neutrino oscillation experiments
- Nonresonant background gives noticeable contribution, especially for neutron target
- Background model based on nonlinear $SU(2)$ sigma-model is implemented in the GiBUU code
- Good agreement with electroproduction data as benchmark for further neutrino calculations. Detailed description of neutrino reactions.